

Learning Target: I can determine continuity *mathematically*.

Find the intervals on which each function is continuous.

$$25) f(x) = \sin\left(\frac{1}{x-\pi}\right)$$

$$26) f(x) = \begin{cases} x+3 & x \leq -4 \\ -x-9 & x > -4 \end{cases}$$

$$27) f(x) = -2\cot(2x) \text{ over } [-\pi, \pi]$$

$$28) f(x) = \begin{cases} -2x+6 & x < 6 \\ -2 & x \geq 6 \end{cases}$$

$$29) f(x) = \frac{x+1}{x^2-4x}$$

$$30) f(x) = \frac{25x}{x^2+25}$$

$$31) f(x) = \begin{cases} -\frac{x}{2}-1 & x \leq 1 \\ -x^2+4x-3 & x > 1 \end{cases}$$

$$32) f(x) = \begin{cases} \frac{x}{2}-3 & x > -4 \\ -x^2-4x-5 & x \leq -4 \end{cases}$$

Learning Target: I can classify types of discontinuities providing a *mathematical* explanation for each.

Determine if each function is continuous. If the function is not continuous, find the x-axis location of and classify each discontinuity.

$$33) f(x) = \begin{cases} x^2-4x+3 & x \geq 3 \\ -2x+3 & x < 3 \end{cases}$$

$$34) f(x) = -\frac{x^2-9x+18}{x-1}$$

$$35) f(x) = \frac{-x-1}{x^2+x+1}$$

$$36) f(x) = \cos\left(\frac{1}{x}\right) \text{ over } [-\pi, \pi]$$

$$37) f(x) = \sin\left(\frac{1}{x+\pi}\right)$$

$$38) f(x) = -\tan(2x) \text{ over } [-\pi, \pi]$$

$$39) f(x) = \frac{x^2-2x-8}{x+2}$$

$$40) f(x) = \begin{cases} -x^2+16x-63 & x \geq 7 \\ -2x+9 & x < 7 \end{cases}$$

Directions: Choose at least 4 problems from each learning target. If you need to do more, do more.

Learning Target: I can find limits using purely algebraically methods. Do not use l'Hôpital's Rule.

$$1) \lim_{x \rightarrow 2} \frac{x^2 - 1}{x^3 + 2} \qquad 2) \lim_{x \rightarrow -2} \frac{x + 2}{x^2 - 4} \qquad 3) \lim_{x \rightarrow -2} \frac{x^2 - 4}{x^3 + 8} \qquad 4) \lim_{x \rightarrow -1} \frac{\frac{1}{x+2} - 1}{x+1}$$

$$5) \lim_{x \rightarrow 0} \frac{\sqrt{x+9} - 3}{x} \qquad 6) \lim_{x \rightarrow 0} \frac{\frac{1}{x+1} - 1}{x} \qquad 7) \lim_{x \rightarrow 1} \frac{\sqrt{3} - \sqrt{x+2}}{1-x} \qquad 8) \lim_{x \rightarrow -2} \frac{x^2 - 1}{2x}$$

Learning Target: I can use the properties of limits to evaluate limits.

For 9-12, use $\lim_{x \rightarrow c} f(x) = 4$ and $\lim_{x \rightarrow c} g(x) = 5$ to evaluate the limits.

$$9) \lim_{x \rightarrow c} [f(x)]^3 \qquad 10) \lim_{x \rightarrow c} [3f(x) - g(x)] \qquad 11) \lim_{x \rightarrow c} [f(x)g(x)] \qquad 12) \lim_{x \rightarrow c} \frac{f(x)}{g(x)}$$

For 13-16, use $\lim_{x \rightarrow c} f(x) = 27$ and $\lim_{x \rightarrow c} g(x) = 12$ to evaluate the limits.

$$13) \lim_{x \rightarrow c} \sqrt[3]{f(x)} \qquad 14) \lim_{x \rightarrow c} \frac{f(x)}{18} \qquad 15) \lim_{x \rightarrow c} [f(x)g(x)] \qquad 16) \lim_{x \rightarrow c} [f(x) - 2g(x)]$$

Learning Target: I can find one-sided and two-sided limits.

$$17) \lim_{x \rightarrow -1^+} (-|x+1| - 1) \qquad 18) \lim_{x \rightarrow -2^-} (x + |2x+4|) \qquad 19) \lim_{x \rightarrow 2^+} f(x), f(x) = \begin{cases} x^2 + 6x + 8, & x \leq -1 \\ -2x + 1, & x > -1 \end{cases} \qquad 20) \lim_{x \rightarrow \frac{\pi}{2}^-} 2 \sec x$$

$$21) \lim_{x \rightarrow 2^+} \frac{x-2}{x^2 - 3x + 2} \qquad 22) \lim_{x \rightarrow 1^+} \frac{x-1}{x^2 - 4x + 3} \qquad 23) \lim_{x \rightarrow 2^+} f(x), f(x) = \begin{cases} x+1, & x \leq 2 \\ \frac{x}{2} + 2, & x > 2 \end{cases} \qquad 24) \lim_{x \rightarrow \frac{\pi}{3}^+} -\cot(2x)$$