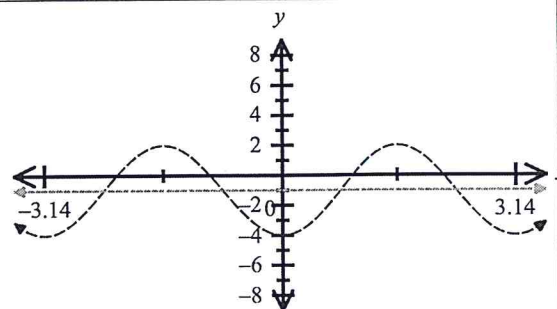


How to Graph Secant and Cosecant:

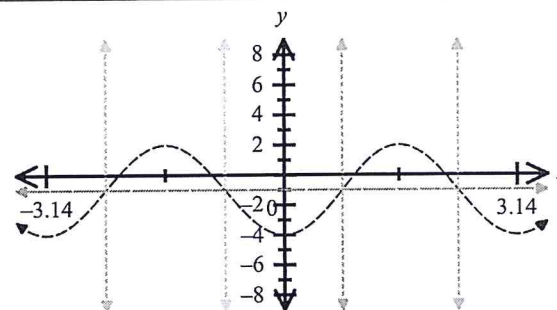
- 1) Graph the underlying sine or cosine graph. Remember that $\sec x = \frac{1}{\cos x}$ and $\csc x = \frac{1}{\sin x}$.
- 2) When the underlying sine/cosine crosses the axis (center line) of its graph, draw a vertical asymptote.
- 3) Plot a point wherever the underlying sine/cosine reaches the high and low points.
- 4) Draw parabola-like shapes between each pair of asymptotes and through the high/low points away from the underlying sine/cosine.

Example: Graph $y = 3 \sec 2\left(x + \frac{\pi}{2}\right) - 1$.

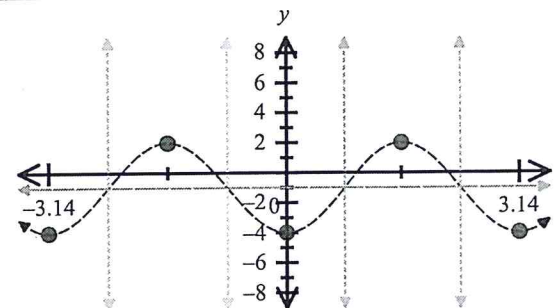
1) Graph $y = 3 \cos 2\left(x + \frac{\pi}{2}\right) - 1$



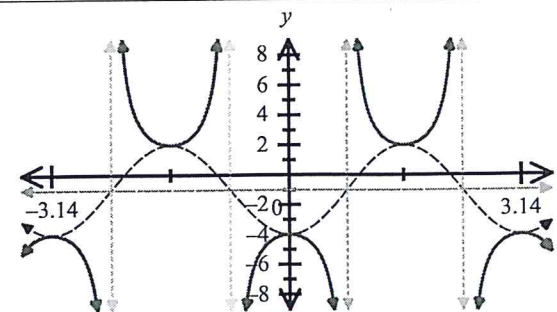
2) Draw asymptotes wherever the cosine crosses the center line...



3) Plot points at high and low points...



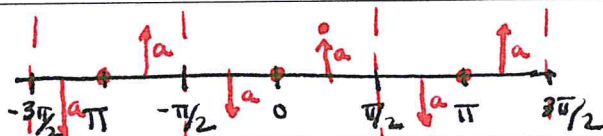
4) Draw the graph...



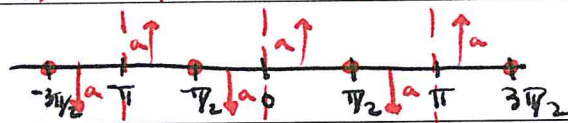
How to Graph Tangent and Cotangent: I will explain why you go through these steps on Monday.

- Remember that $\tan x = \frac{\sin x}{\cos x}$ and $\cot x = \frac{\cos x}{\sin x}$. Find amplitude "a" and axis "k".
- Graph the axis $y = "k"$.
- Set the denominator (either sine or cosine) equal to 0 and solve for x. This gives you where the vertical asymptotes are. Plot them.
- Plot a point on the axis at every midpoint between the asymptotes. These represent "roots" of the tan/cot curve.
- Find the midpoint between the "roots" and asymptotes. What you do here depends on if it's a tangent or cotangent:

a) Tangent:



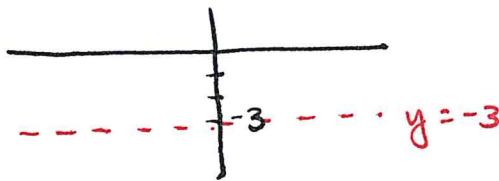
b) Cotangent:



6) Draw the graph.

Example: Graph $y = 2 \cot(2x - \pi) - 3$

1 & 2) $a = 2$ and axis $(k) = -3$



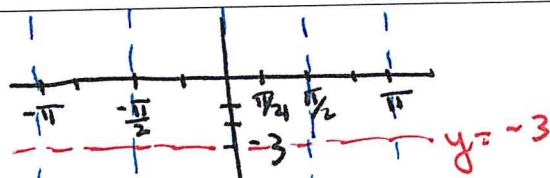
3) Set denominator = 0 and solve for asymptotes. Plot them.

$$\cot = \frac{\cos}{\sin}$$

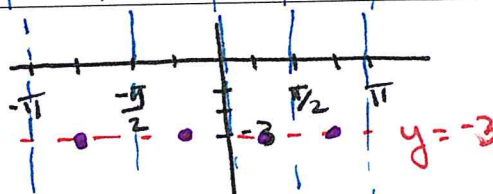
$$\sin(2x - \pi) = 0$$

$$2x - \pi = 0, \pi, 2\pi, 3\pi, \dots$$

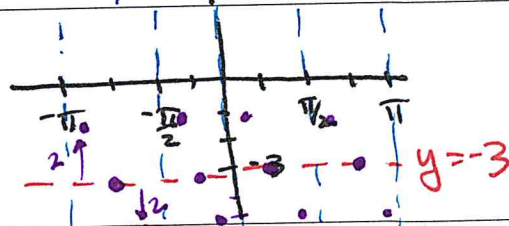
$$\begin{aligned} 2x &= \pi, 2\pi, 3\pi, 4\pi, \dots \\ x &= \frac{\pi}{2}, \pi, \frac{3\pi}{2}, 2\pi, \dots \end{aligned}$$



4) Plot midpoints between asymptotes on axis.



5) Find midpoints and plot amplitude for cot.



6) Draw the graph.

